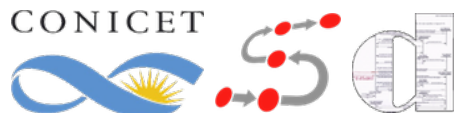


# Optimal Routing in Satellite DTN through Markov Decision Processes

Pedro R. D'Argenio

Joint work with

Juan Fraire, Arnd Hartmanns, Fernando Raverta,  
Ramiro Demasi, Pablo Madhoery, Jorge Finochieto

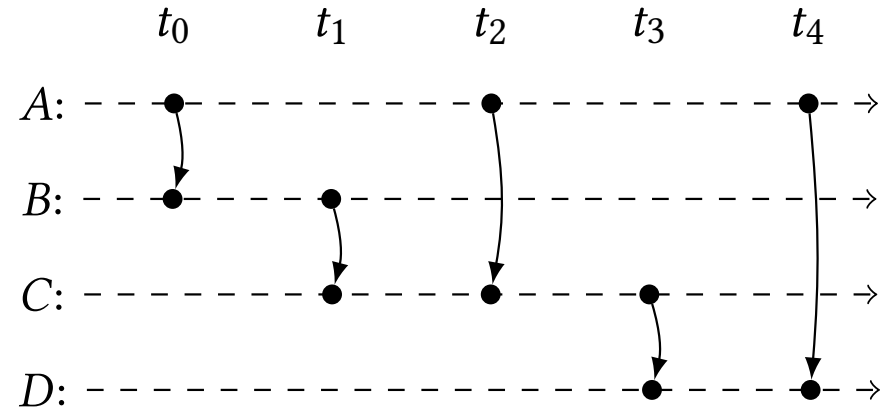
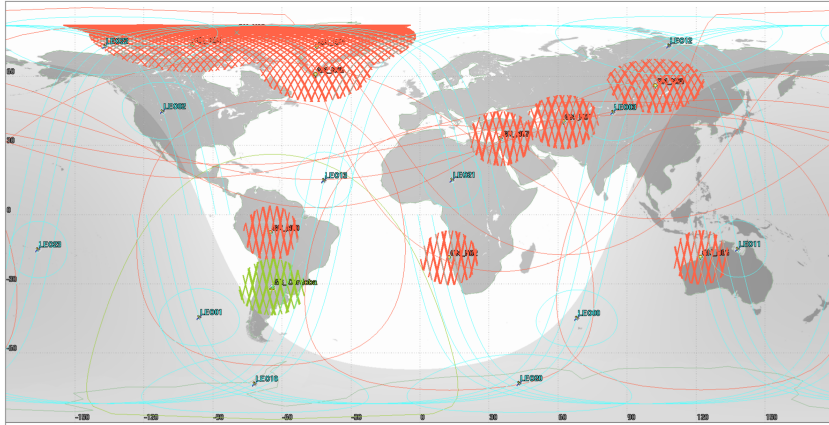


MISSION@INVAP - February 2022

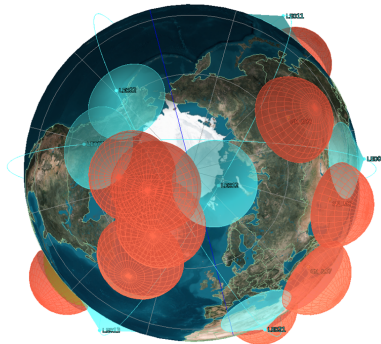
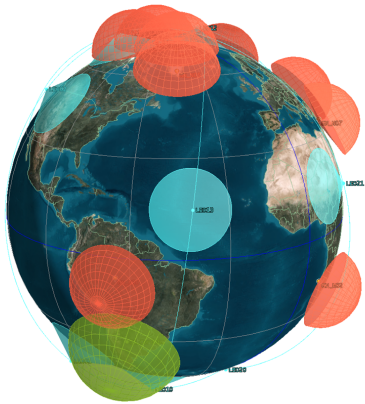


# Satellite Delay Tolerant Networks

Contact Plan

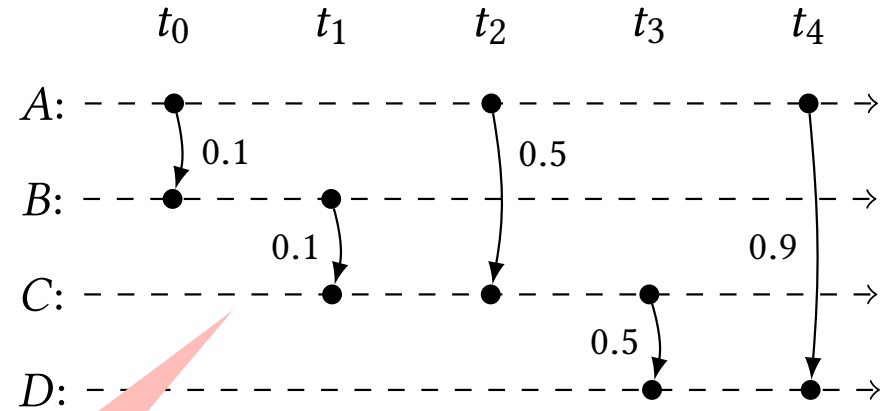
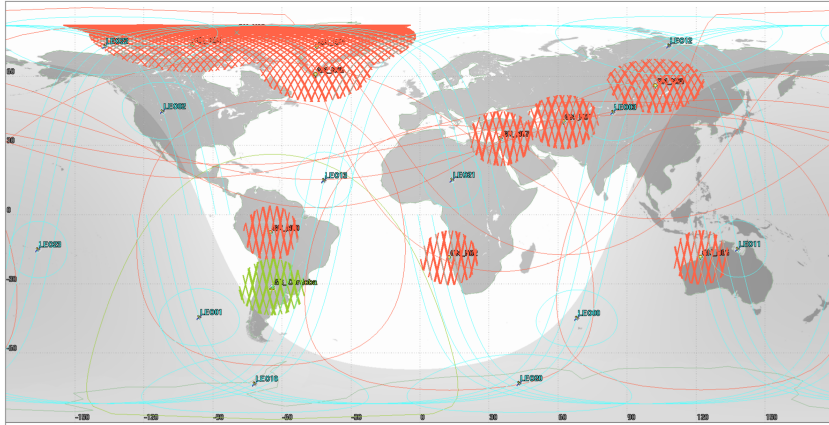


Standard: Contact Graph Routing (CGR)



# Satellite Delay Tolerant Networks

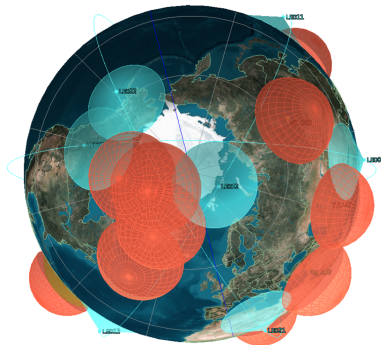
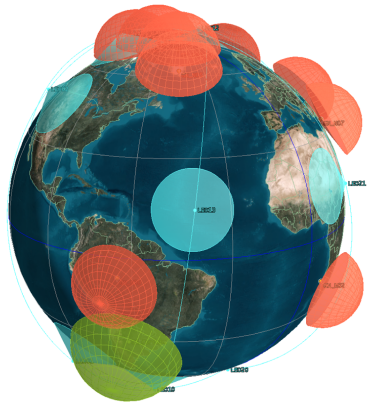
Contact Plan



Links may fail!

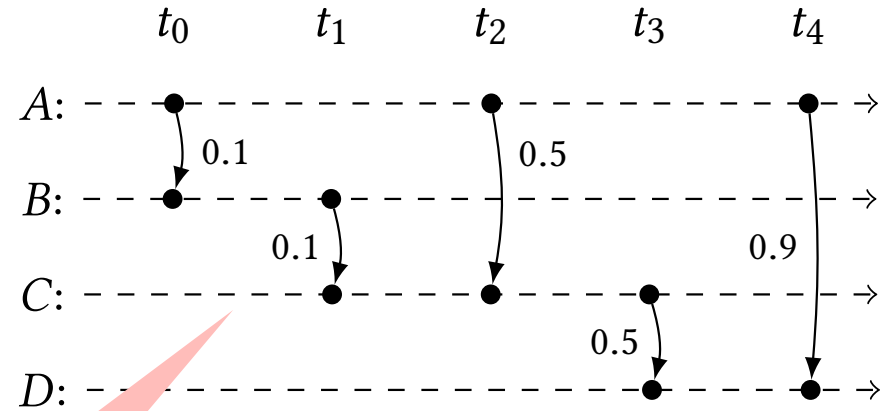
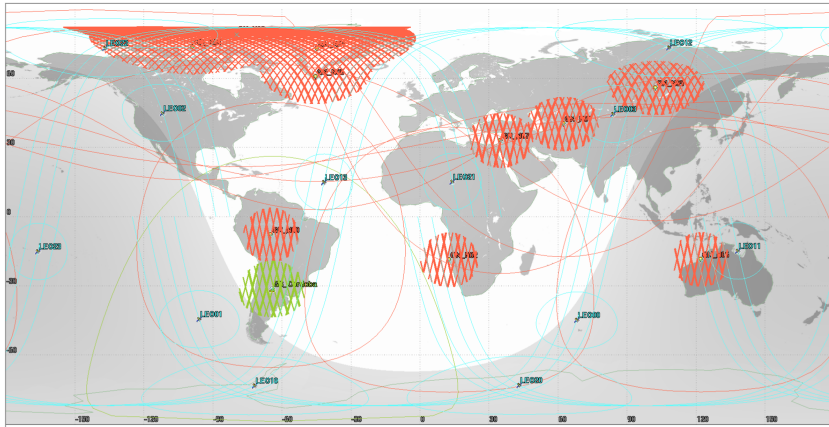
Standard: Contact Graph Routing (CGR)

Increase reliability: CGR with multiple copies



# Satellite Delay Tolerant Networks

Contact Plan

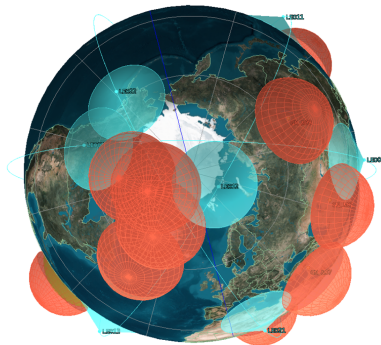
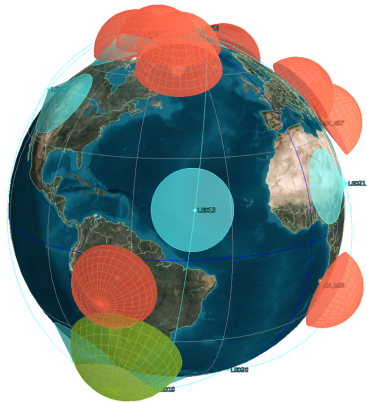


Links may fail!

Not optimal!

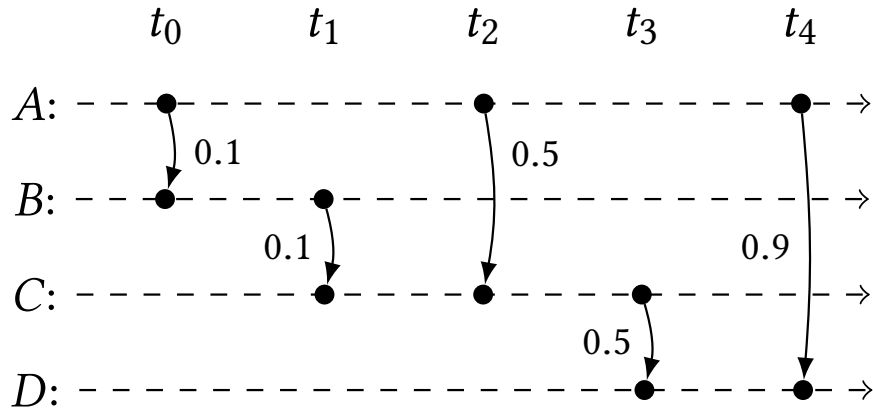
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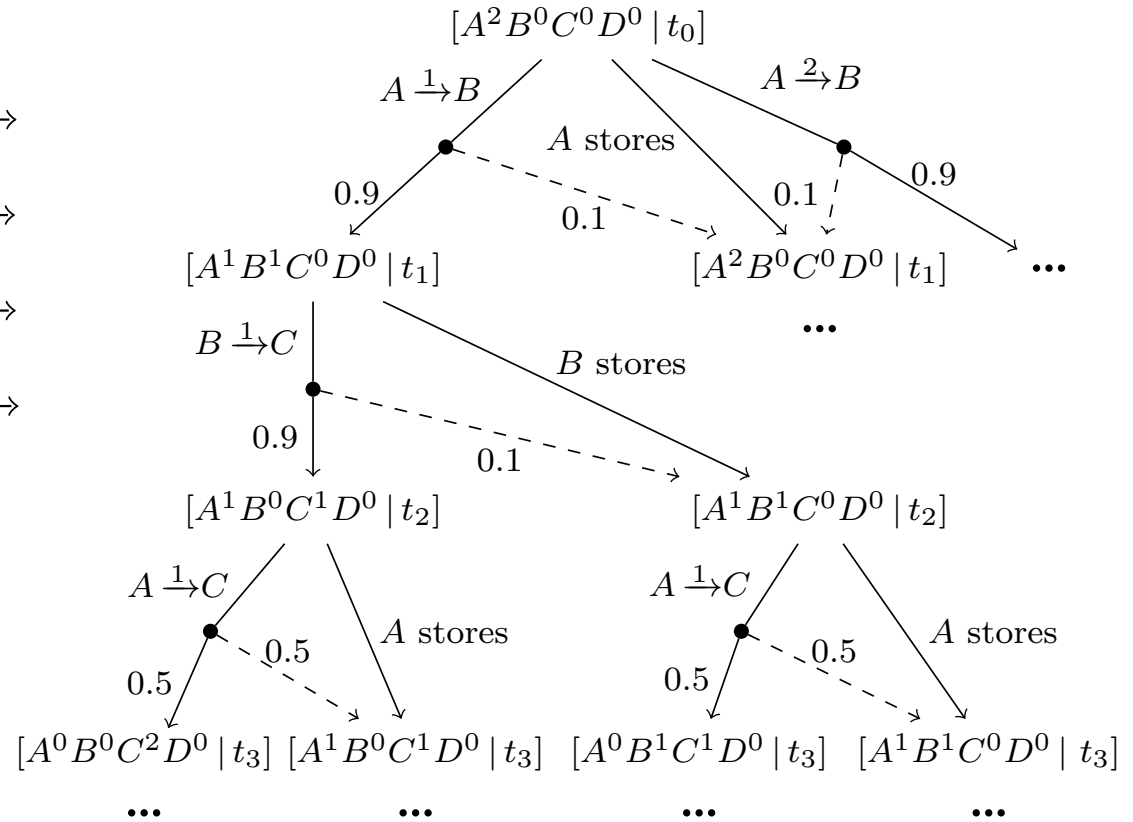




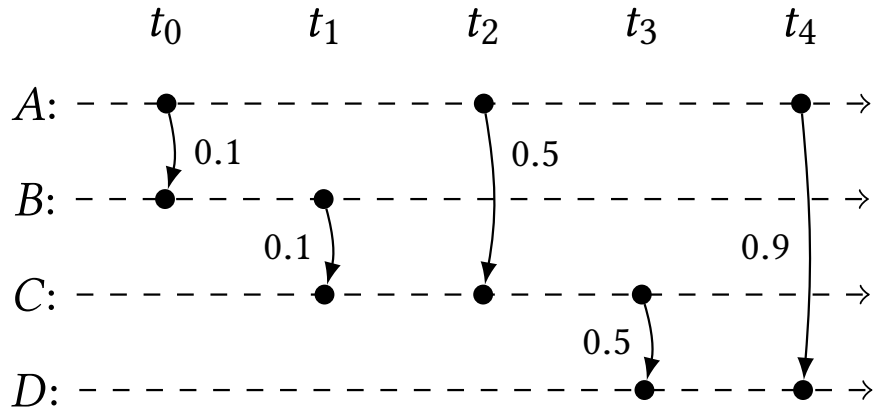
# Optimality through Markov Decision Processes



Assume 2 copies are sent

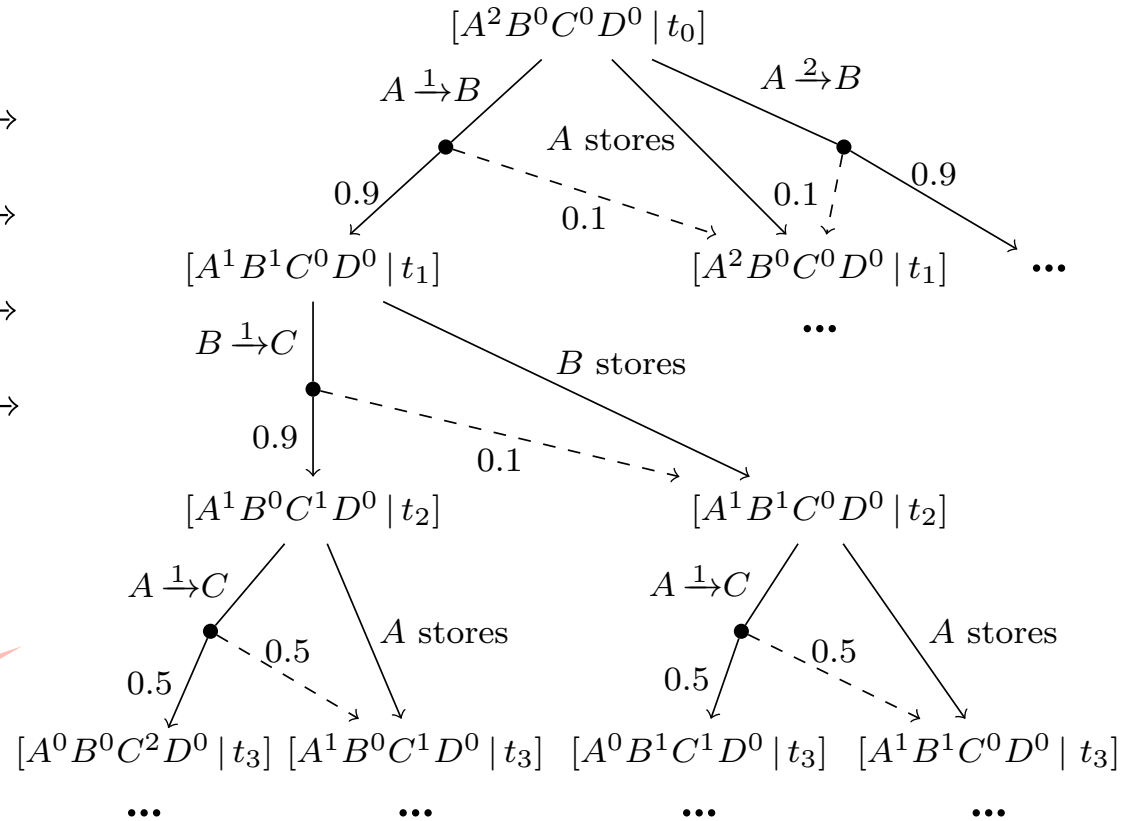


# Optimality through Markov Decision Processes

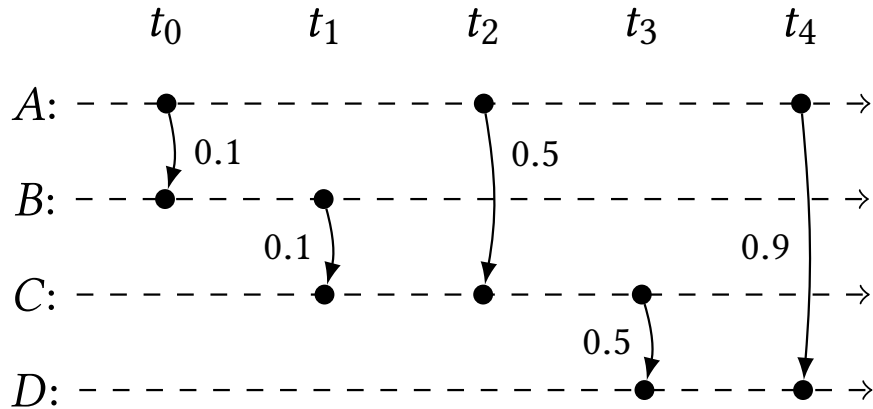


Assume 2 copies are sent

We have a **reachability problem** where goal states are those with a copy at target node

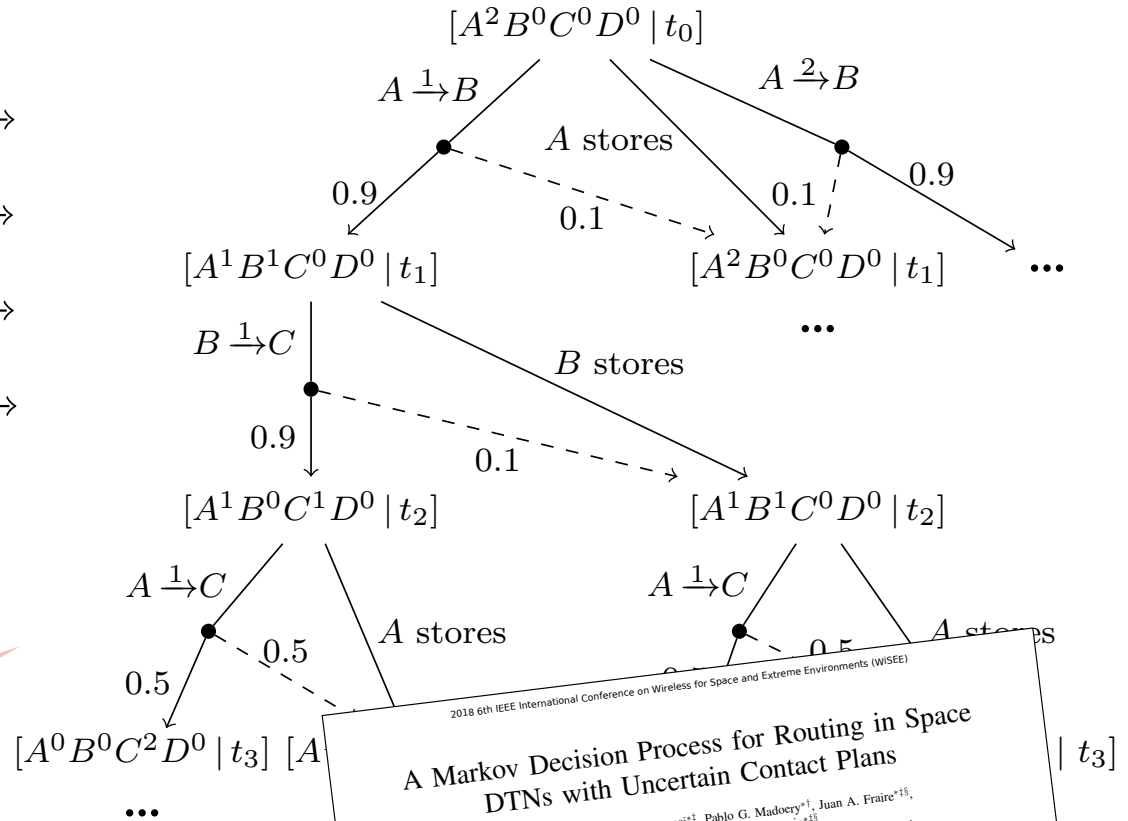


# Optimality through Markov Decision Processes



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2018 6th IEEE International Conference on Wireless for Space and Extreme Environments (WISEE)

### A Markov Decision Process for Routing in Space DTNs with Uncertain Contact Plans

Fernando D. Raverta<sup>+</sup>, Ramiro Demasi<sup>+</sup>, Pablo G. Madoery<sup>†</sup>, Juan A. Fraire<sup>‡§</sup>, Jorge M. Finochietto<sup>†</sup>, Pedro R. D'Argenio<sup>‡§</sup>

<sup>+</sup>Consejo Nacional de Investigaciones Científicas y Técnicas (CONICET), Córdoba, Argentina  
<sup>†</sup>Facultad de Ciencias Exactas, Físicas y Naturales (FCEFN), UNC, Córdoba, Argentina  
<sup>‡</sup>Facultad de Matemática, Astronomía, Física y Computación (FAMAF), UNC, Córdoba, Argentina  
<sup>§</sup>Department of Computer Science, Saarland University, Saarbrücken, Germany

**Abstract**—Delay Tolerant Networking (DTN) has been proposed to provide efficient and autonomous store-carry-and-forward data transport for space-terrestrial networks. Since these networks rely on scheduled contact plans, Contact Graph (CG) can be used to optimize routing and data delivery, considering uncertainties and faults in the contact plan. In this paper, we consider different types of deterministic DTNs are known as scheduled DTNs and can take advantage of a contact plan comprising the future network connectivity in order to optimize data forwarding. However, scheduled routing solutions such as Contact Graph Routing (CGR) assumes the estimation of the future topology status is highly accurate [3]. Indeed, CGR consider scheduling uncertainties such as transient contact plan changes and contact pointing inaccuracies

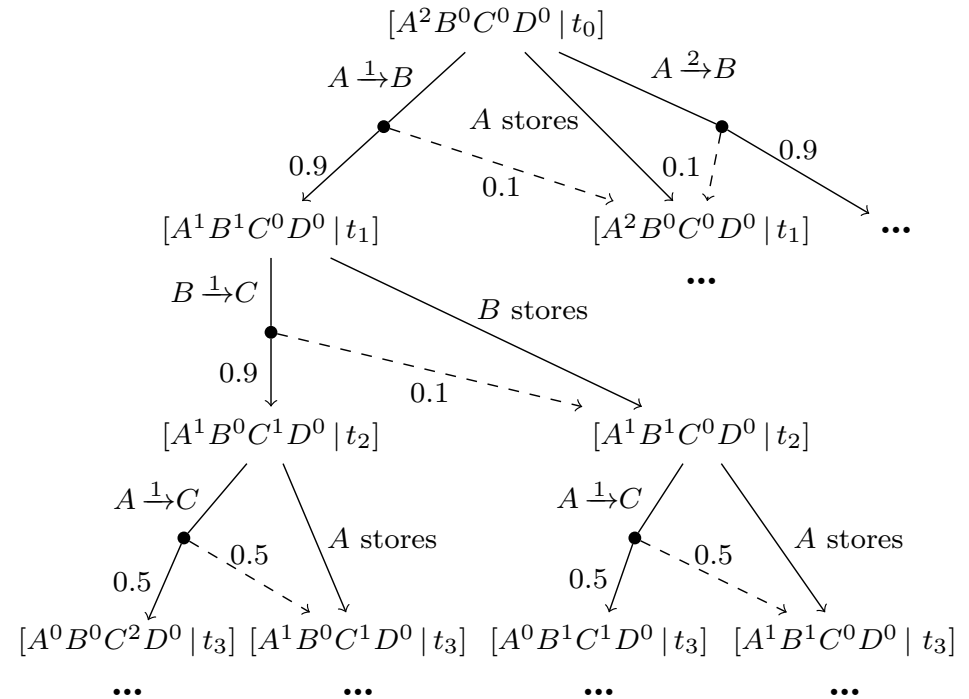
First technique

# Routing under Uncertain Contact Plans (RUCoP)

Observe: **MDP (almost) acyclic**

**RUCoP:**

- ❖ follows Bellman equations backwardly (starting from goal states)
- ❖ only one pass required
- ❖ only maximizing subgraph (Markov chain!) is preserved



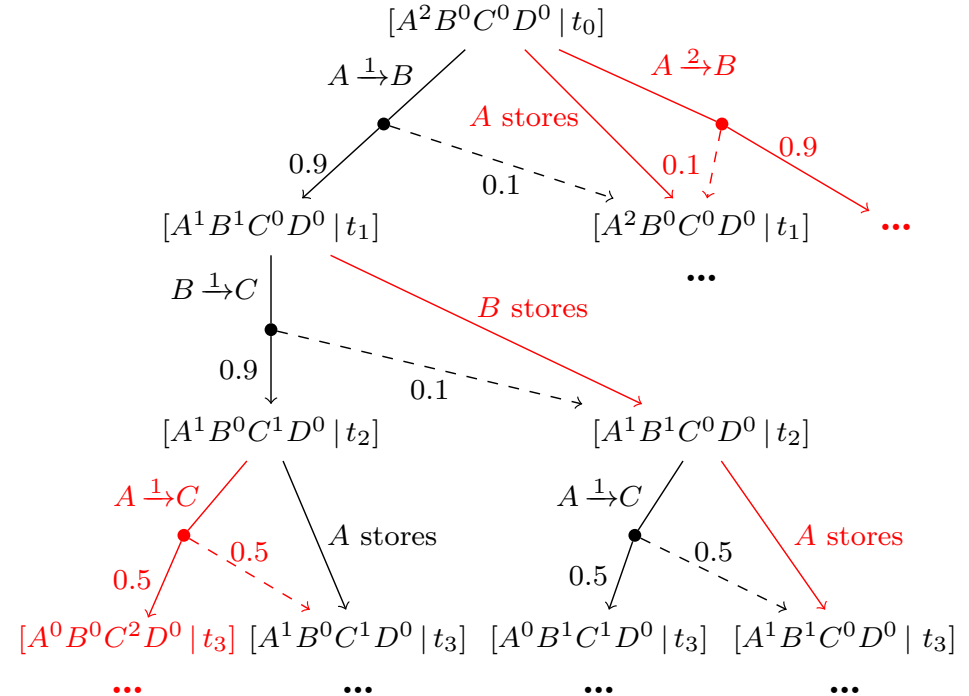
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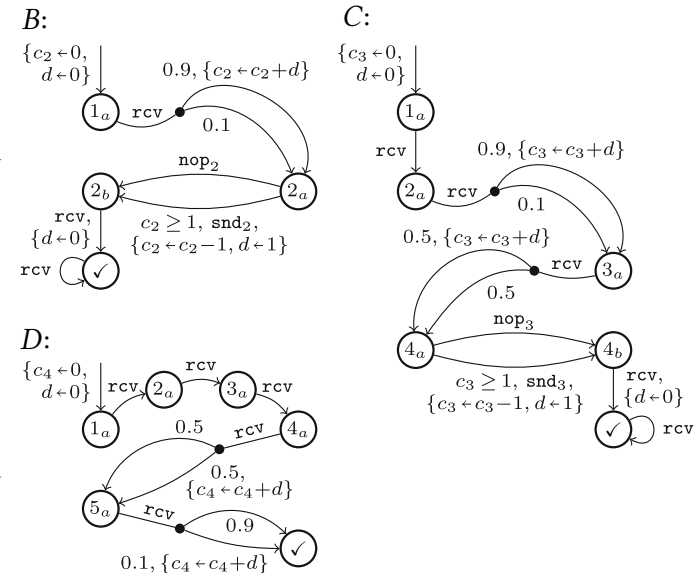
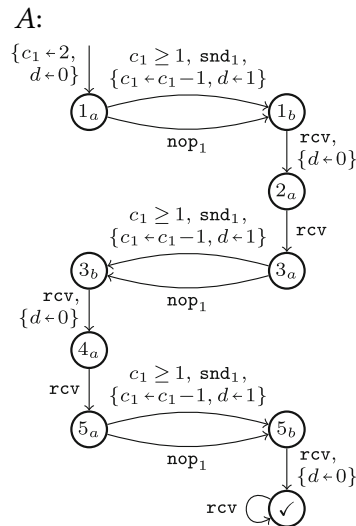
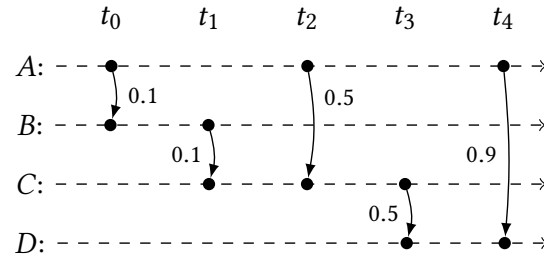




# Simulation through Lightweight Smart Sampling (LSS)

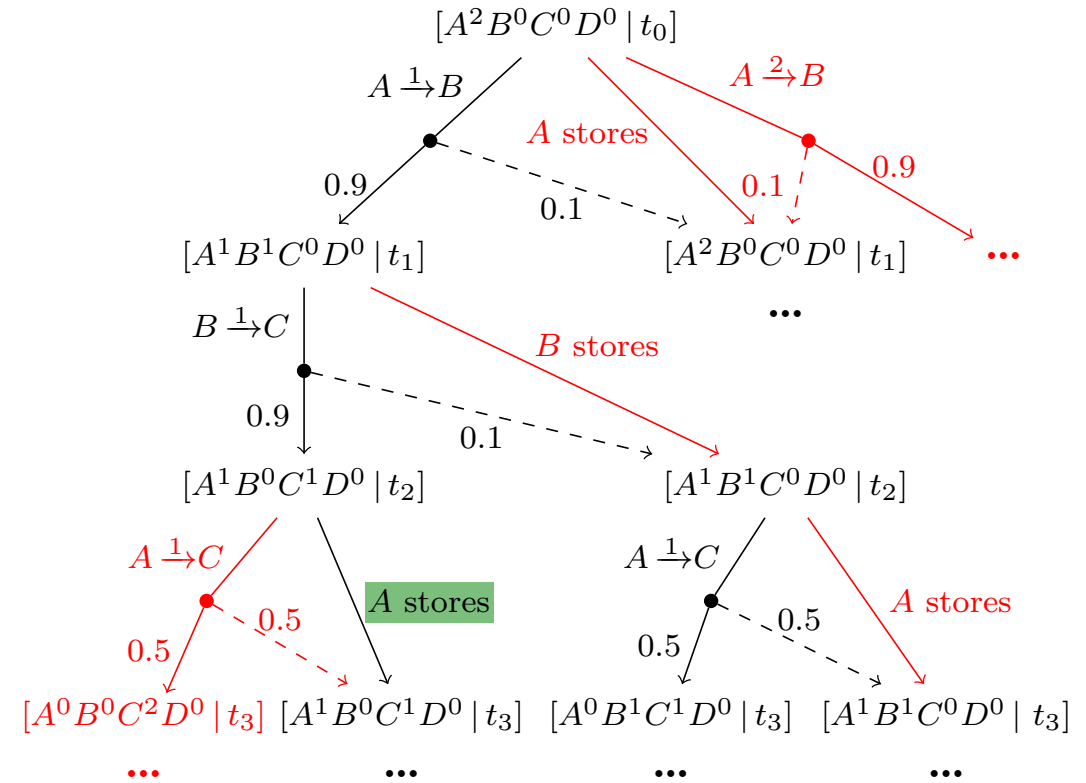
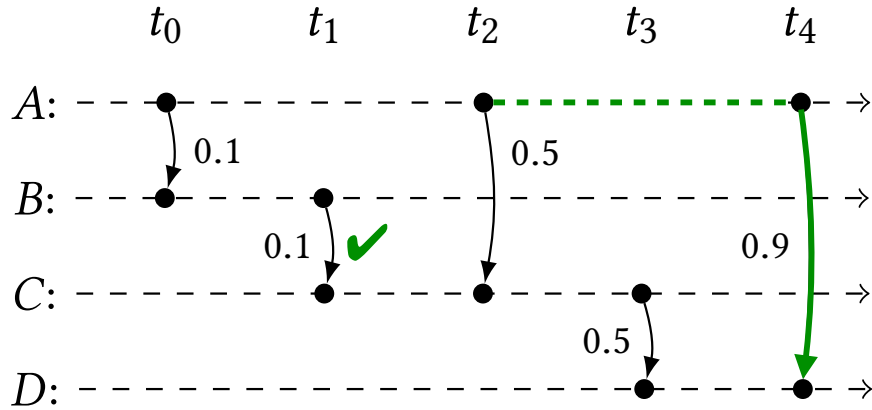
SMC+LSS:

1. Select  $m$  32-bit integer, each of them representing a scheduler identifier  $\sigma$
  2. For each  $\sigma$ , perform standard SMC letting  $\sigma$  resolve all non-determinism
  3. Return the maximum (or minimum) and the corresponding  $\sigma$
- ❖ SMC+LSS returns an underapproximation (or overapproximation) which we call **near optimal**
  - ❖ The efficiency depends on  $m$

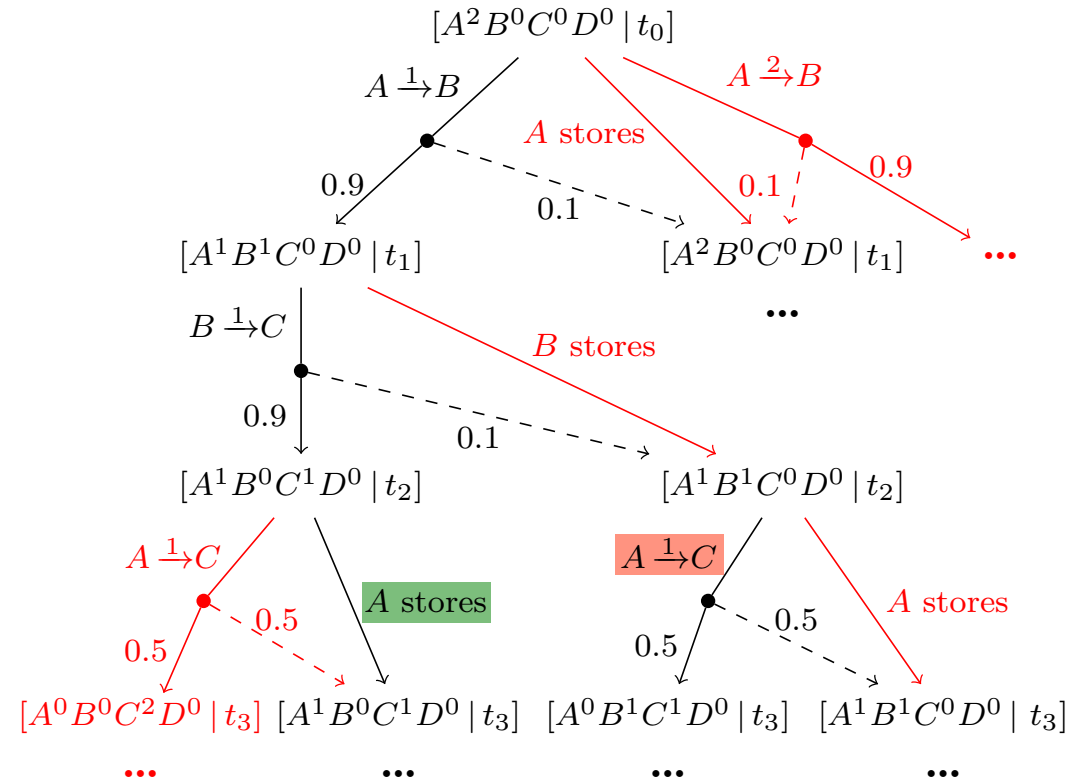
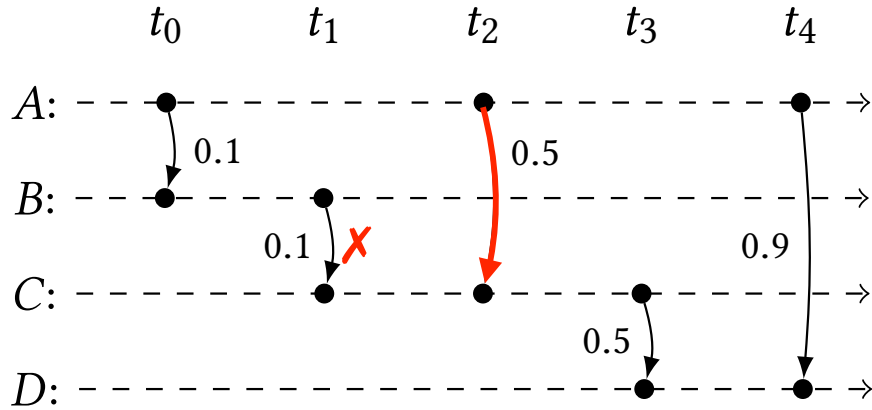


Implemented in the **MODEST** toolset

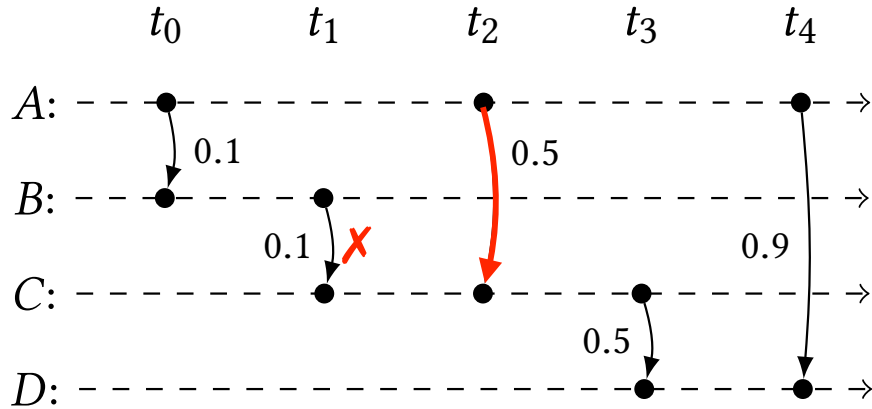
# The problem of distributed information



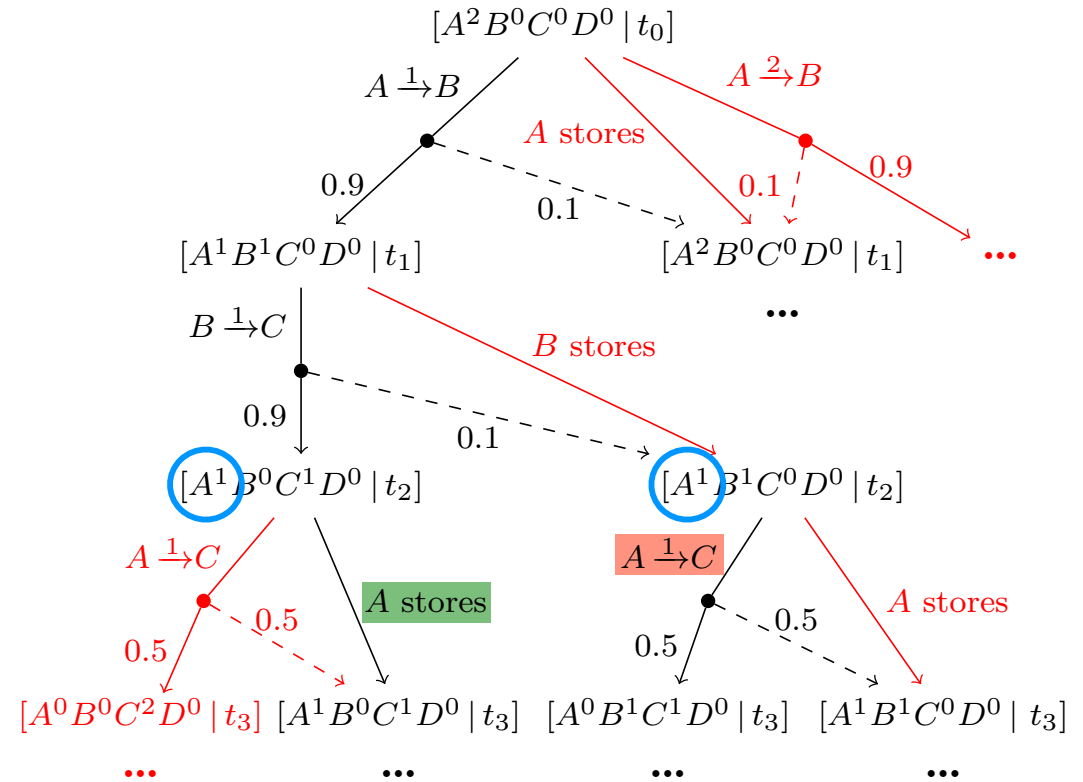
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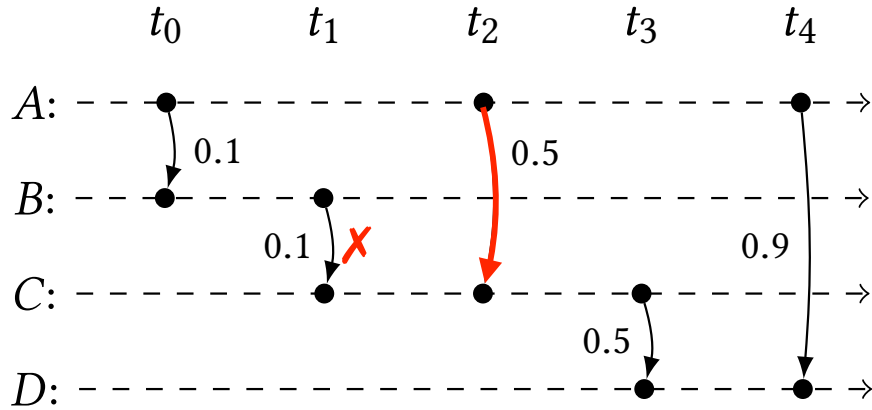
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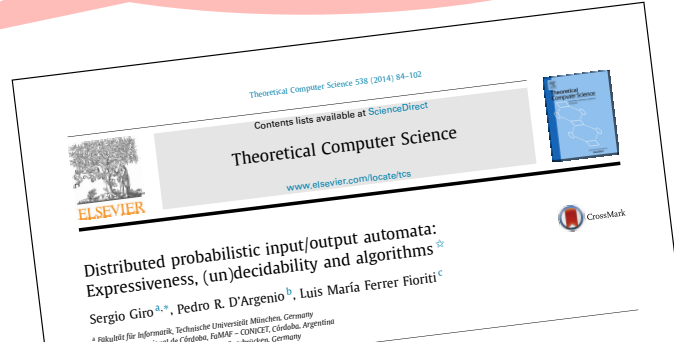
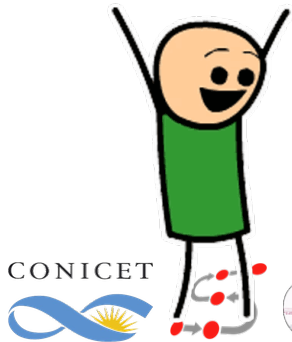
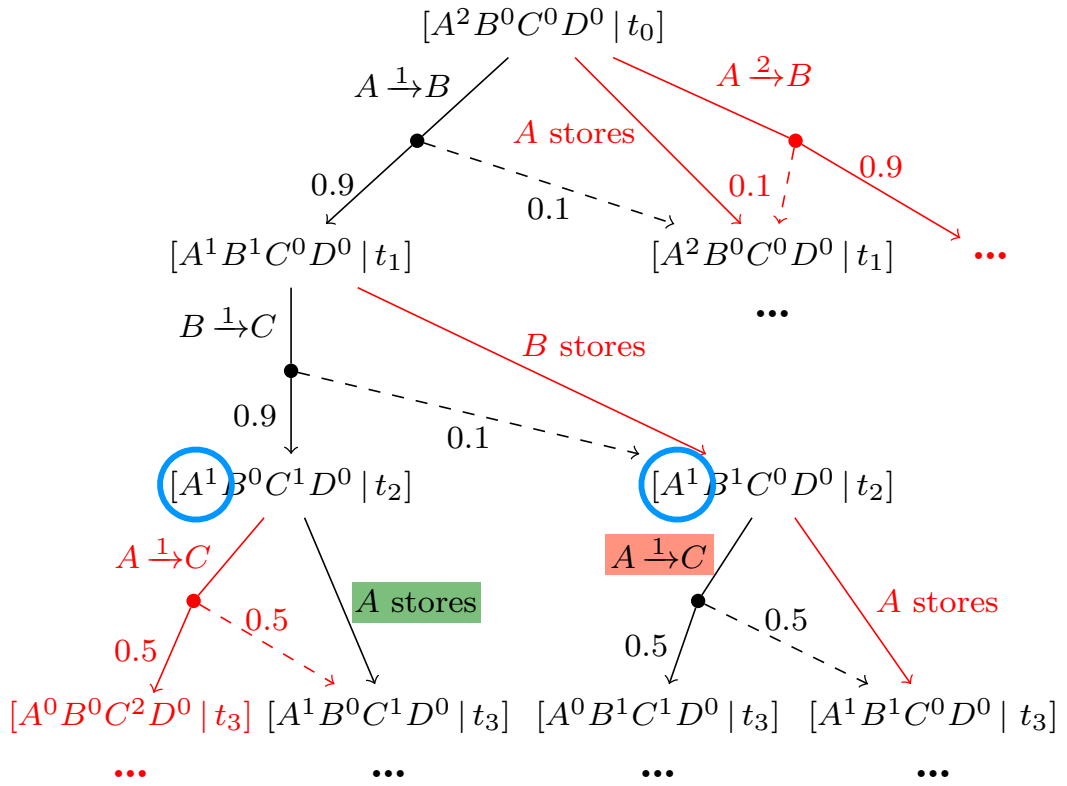
The decision has to be the same regardless the occurrences of locally unknown events



# The problem of distributed information



Luckily we have distributed schedulers





# Third technique

## Local decisions using RUCoP (L-RUCoP)

**Input:** number of copies  $N$ , target node  $T$

**Output:** A routing table  $LTr_n$  for each node  $n$

```
1: for all  $c \leq N$  do
2:    $(S_c, Tr_c, Pr_c) \leftarrow RUCoP(G, c, T)$ 
3: end for
4: for all node  $n$ , time slot  $ts$ , and  $c \leq N$  do
5:    $s \leftarrow Safe\_state(n, c, ts)$ 
6:   if  $s \in S_c$  then
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10:    while  $rc > 0$  do
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Construct all RUCoP  
tables for  $c \leq N$

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```

Start from a **safe state**  
for node  $n$  with  $c$  copies at  
time slot  $ts$

$$Safe\_state(A, 2, t_0) = [A^2 B^0 C^0 D^0 \mid t_0]$$

$$Safe\_state(A, 1, t_2) = [A^1 B^0 C^0 D^0 \mid t_2]$$

# Third technique

## Local decisions using RUCoP (L-RUCoP)

**Input:** number of copies  $N$ , target node  $T$

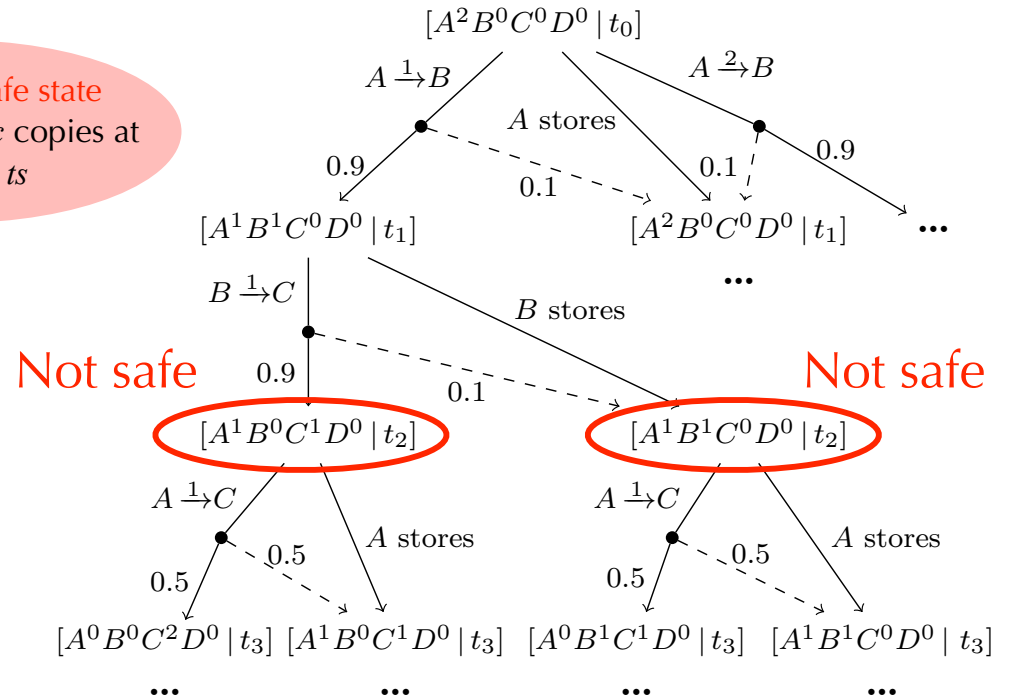
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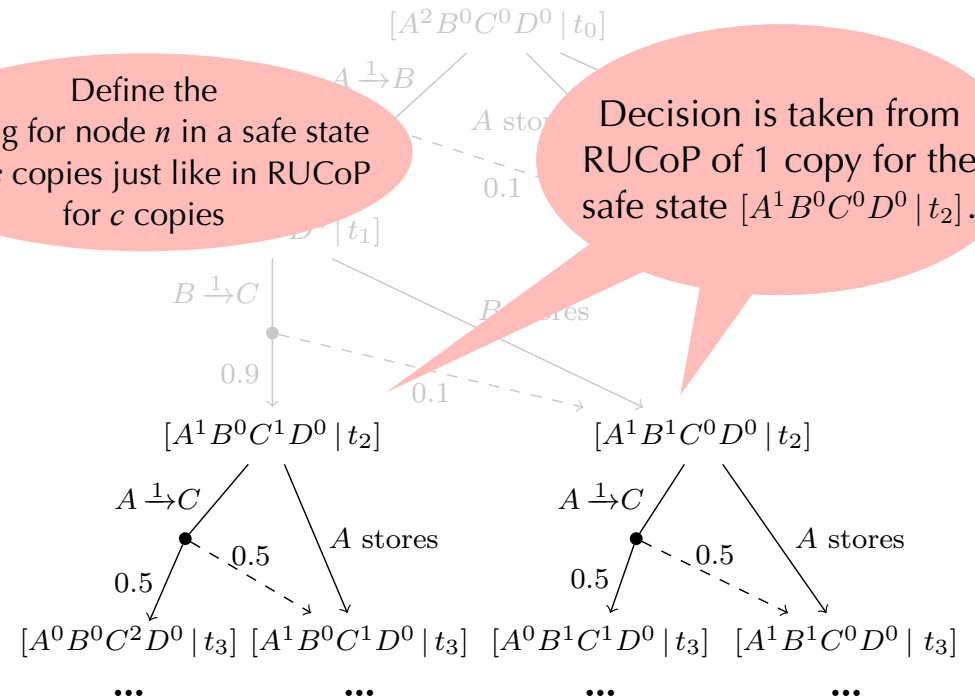
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```

Define the routing for node  $n$  in a safe state with  $c$  copies just like in RUCoP for  $c$  copies

Decision is taken from RUCoP of 1 copy for the safe state  $[A^1 B^0 C^0 D^0 \mid t_2]$ .





# Third technique

## Local decisions using RUCoP (L-RUCoP)

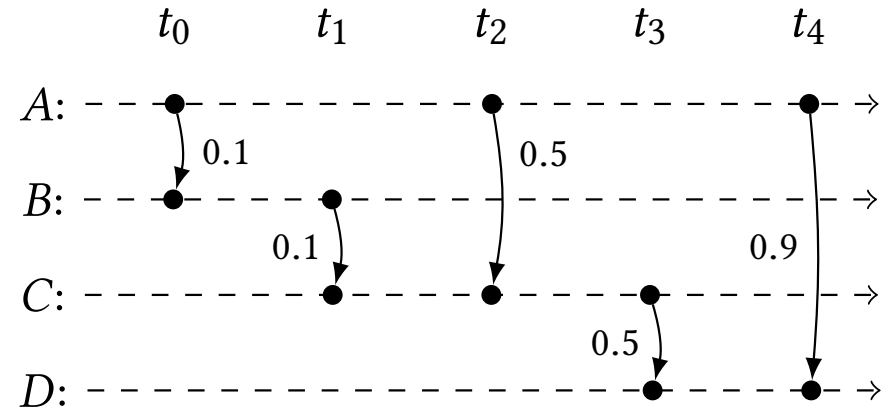
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Sometimes a node has some information about other nodes (e.g. when it just sent a message)

# Third technique

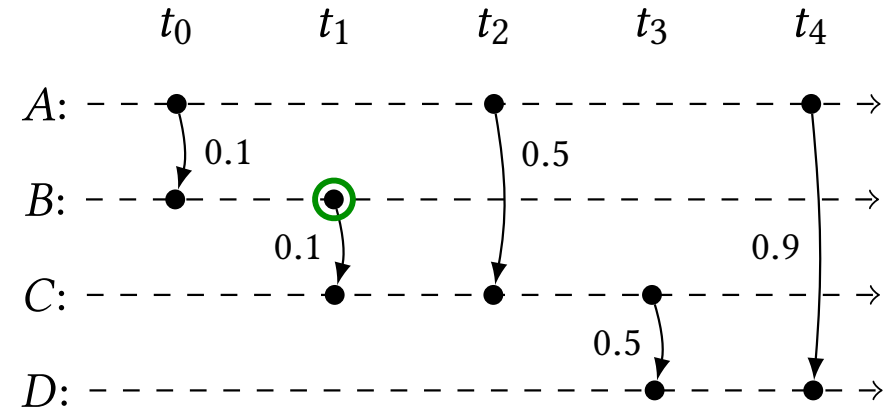
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```



$t_1$ :  $B$  sends a copy to  $C$  who ack reception

Sometimes a node has some information about other nodes (e.g. when it just sent a message)

# Third technique

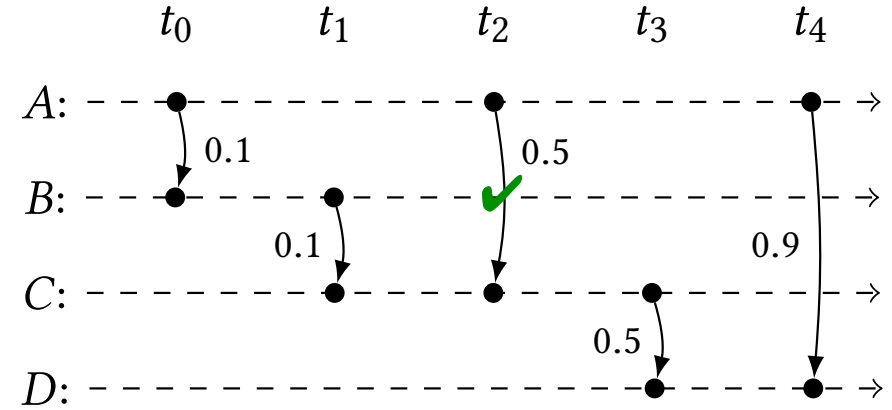
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6:   if  $s \in S_c$  then
7:      $LTr_n(ts, c, ts) \leftarrow \{(k, r) \in Tr_c(s) \mid first(r) = n\}$ 
8:      $ts' \leftarrow ts$ 
9:      $rc \leftarrow (\exists (k, n) \in LTr_r(n, ts, c, ts'))? k : 0$ 
10:    while  $rc > 0$  do
11:       $s' \leftarrow Post(LTr_n(ts, rc, ts'))$ 
12:       $ts' = ts' + 1$ 
13:      if  $s' \in S_{rc}$  then
14:         $LTr_n(ts, rc, ts') \leftarrow \{(k, r) \in Tr_{rc}(s') \mid first(r) = n\}$ 
15:      else
16:        break
17:      end if
18:       $rc \leftarrow (\exists (k, n) \in LTr_n(ts, rc, ts'))? k : 0$ 
19:    end while
20:  end if
21: end for
22: return  $LTr_n$ , for all node  $n$ .
  
```



$t_2$ : B knows C has a copy

Sometimes a node has some information about other nodes (e.g. when it just sent a message)

# Third technique

## Local decisions using RUCoP (L-RUCoP)

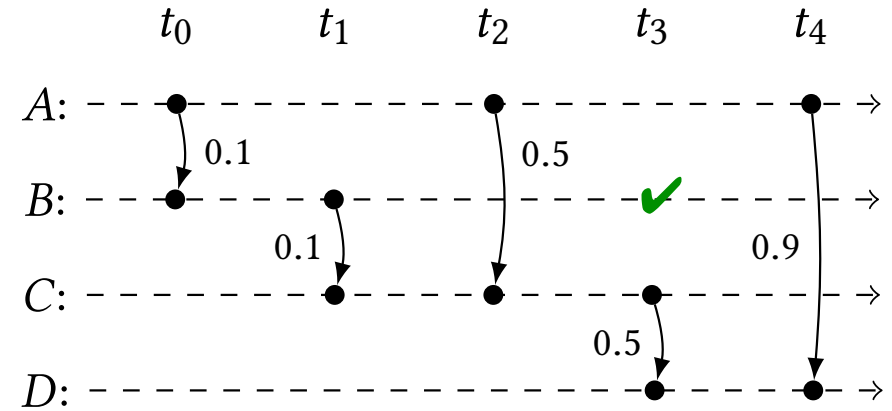
**Input:** number of copies  $N$ , target node  $T$

**Output:** A routing table  $LTr_n$  for each node  $n$

```

1: for all  $c \leq N$  do
2:    $(S_c, Tr_c, Pr_c) \leftarrow RUCoP(G, c, T)$ 
3: end for
4: for all node  $n$ , time slot  $ts$ , and  $c \leq N$  do
5:    $s \leftarrow Safe\_state(n, c, ts)$ 
6:   if  $s \in S_c$  then
7:      $LTr_n(ts, c, ts) \leftarrow \{(k, r) \in Tr_c(s) \mid first(r) = n\}$ 
8:      $ts' \leftarrow ts$ 
9:      $rc \leftarrow (\exists (k, n) \in LTr_r(n, ts, c, ts'))? k : 0$ 
10:    while  $rc > 0$  do
11:       $s' \leftarrow Post(LTr_n(ts, rc, ts'))$ 
12:       $ts' = ts' + 1$ 
13:      if  $s' \in S_{rc}$  then
14:         $LTr_n(ts, rc, ts') \leftarrow \{(k, r) \in Tr_{rc}(s') \mid first(r) = n\}$ 
15:      else
16:        break
17:      end if
18:       $rc \leftarrow (\exists (k, n) \in LTr_r(n, ts, rc, ts'))? k : 0$ 
19:    end while
20:  end if
21: end for
22: return  $LTr_n$ , for all node  $n$ .

```



$t_3$ : B knows C has a copy

Sometimes a node has some information about other nodes (e.g. when it just sent a message)

# Third technique

## Local decisions using RUCoP (L-RUCoP)

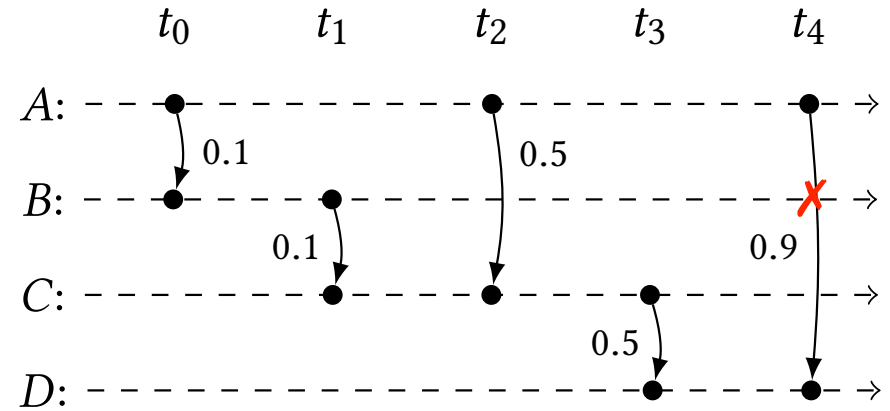
**Input:** number of copies  $N$ , target node  $T$

**Output:** A routing table  $LTr_n$  for each node  $n$

```

1: for all  $c \leq N$  do
2:    $(S_c, Tr_c, Pr_c) \leftarrow RUCoP(G, c, T)$ 
3: end for
4: for all node  $n$ , time slot  $ts$ , and  $c \leq N$  do
5:    $s \leftarrow Safe\_state(n, c, ts)$ 
6:   if  $s \in S_c$  then
7:      $LTr_n(ts, c, ts) \leftarrow \{(k, r) \in Tr_c(s) \mid first(r) = n\}$ 
8:      $ts' \leftarrow ts$ 
9:      $rc \leftarrow (\exists (k, n) \in LTr_r(n, ts, c, ts'))? k : 0$ 
10:    while  $rc > 0$  do
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12:       $ts' = ts' + 1$ 
13:      if  $s' \in S_{rc}$  then
14:         $LTr_n(ts, rc, ts') \leftarrow \{(k, r) \in Tr_{rc}(s') \mid first(r) = n\}$ 
15:      else
16:        break
17:      end if
18:       $rc \leftarrow (\exists (k, n) \in LTr_r(n, ts, rc, ts'))? k : 0$ 
19:    end while
20:  end if
21: end for
22: return  $LTr_n$ , for all node  $n$ .

```



$t_4$ :  $B$  does not know if  $C$  has a copy

Sometimes a node has some information about other nodes (e.g. when it just sent a message)



# Third technique

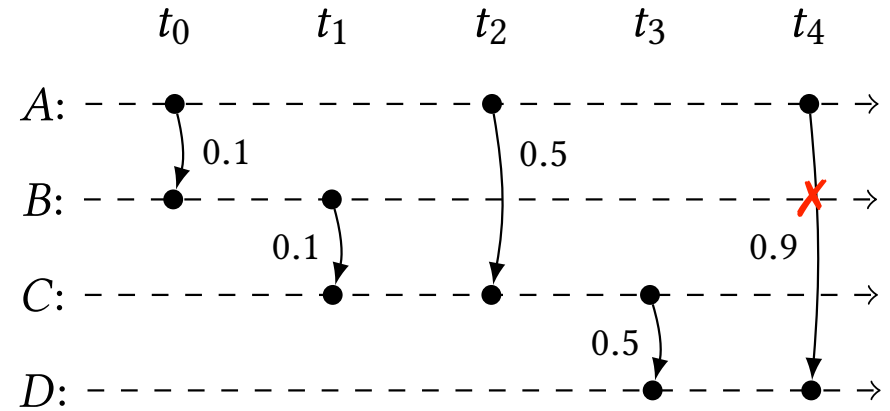
## Local decisions using RUCoP (L-RUCoP)

**Input:** number of copies  $N$ , target node  $T$

**Output:** A routing table  $LTr_n$  for each node  $n$

```

1: for all  $c \leq N$  do
2:    $(S_c, Tr_c, Pr_c) \leftarrow RUCoP(G, c, T)$ 
3: end for
4: for all node  $n$ , time slot  $ts$ , and  $c \leq N$  do
5:    $s \leftarrow Safe\_state(n, c, ts)$ 
6:   if  $s \in S_c$  then
7:      $LTr_n(ts, c, ts) \leftarrow \{(k, r) \in Tr_c(s) \mid first(r) = n\}$ 
8:      $ts' \leftarrow ts$ 
9:      $rc \leftarrow (\exists (k, n) \in LTr_r(n, ts, c, ts'))? k : 0$ 
10:    while  $rc > 0$  do
11:       $s' \leftarrow Post(LTr_n(ts, rc, ts'))$ 
12:       $ts' = ts' + 1$ 
13:      if  $s' \in S_{rc}$  then
14:         $LTr_n(ts, rc, ts') \leftarrow \{(k, r) \in Tr_{rc}(s') \mid first(r) = n\}$ 
15:      else
16:        break
17:      end if
18:       $rc \leftarrow (\exists (k, n) \in LTr_n(ts, rc, ts'))? k : 0$ 
19:    end while
20:  end if
21: end for
22: return  $LTr_n$ , for all node  $n$ .
  
```



$t_4$ :  $B$  does not know if  $C$  has a copy

# Third technique

## Local decisions using RUCoP (L-RUCoP)

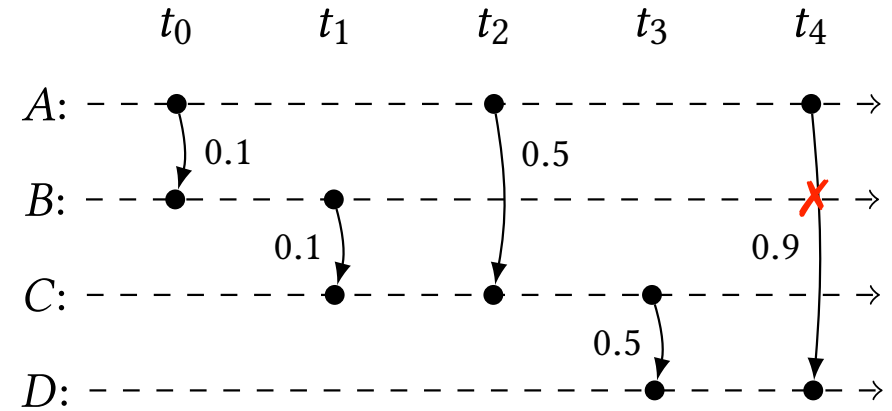
**Input:** number of copies  $N$ , target node  $T$

**Output:** A routing table  $LTr_n$  for each node  $n$

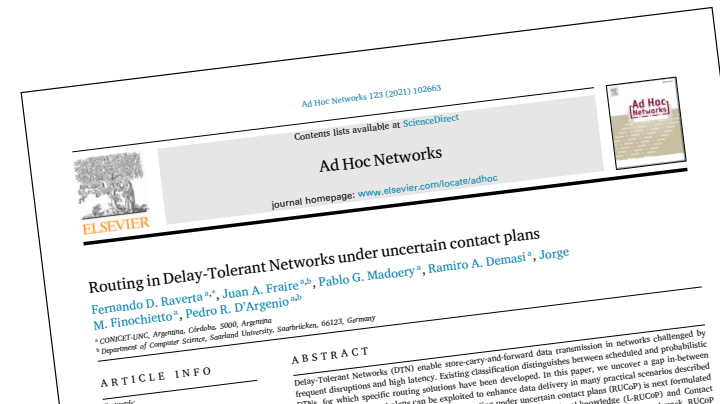
```

1: for all  $c \leq N$  do
2:    $(S_c, Tr_c, Pr_c) \leftarrow RUCoP(G, c, T)$ 
3: end for
4: for all node  $n$ , time slot  $ts$ , and  $c \leq N$  do
5:    $s \leftarrow Safe\_state(n, c, ts)$ 
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19:    end while
20:  end if
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```



$t_4$ :  $B$  does not know if  $C$  has a copy



# Fourth technique

## SMC + LSS of distributed schedulers

- ❖ Resolving non-determinism in SMC+LSS

$$\mathcal{H}(\sigma.s) \bmod n$$

32-bit  
hash function

state as a  
bit vector

number of  
choices at  $s$

# Fourth technique

## SMC + LSS of distributed schedulers

- ❖ Resolving non-determinism in SMC+LSS

$$\mathcal{H}(\sigma.s) \bmod n$$

- ❖ Resolving non-determinism in SMC+LSS+DS

$$\mathcal{H}(\sigma.(s \downarrow_{M_i})) \bmod n_i$$

bit vector limited  
to component  $i$

number of choices of  
component  $i$  at  $s$

# Fourth technique

## SMC + LSS of distributed schedulers

- ❖ Resolving non-determinism in SMC+LSS

$$\mathcal{H}(\sigma.s) \bmod n$$

- ❖ Resolving non-determinism in SMC+LSS+DS

$$\mathcal{H}(\sigma.(s \downarrow_{M_i})) \bmod n_i$$

bit vector limited  
to component  $i$

number of choices of  
component  $i$  at  $s$

**Input:** Network of VMDP  $M = \parallel_{SV} (M_1, \dots, M_n)$  with  $\llbracket M \rrbracket = \langle S, s_I, A, T \rangle$ ,  
goal set  $G \subseteq S$ ,  $\sigma \in \mathbb{Z}_{32}$ ,  $\mathcal{H}$  uniform deterministic, PRNG  $\mathcal{U}_{pr}$ .

```

1  $s := s_I$ 
2 while  $s \notin G$  do // break on goal state
3   if  $\forall s \xrightarrow{a} \mu: \mu = \{s \mapsto 1\}$  then break // break on self-loops
4    $C := \{j \mid T(s) \cap I_t(M_j) \neq \emptyset\}$  // get active components
5    $i := \mathcal{U}_{pr}(\{j \mapsto \frac{1}{|C|} \mid j \in C\})$  // select component uniformly
6    $T_i := T(s) \cap I_t(M_i)$  // get component's transitions
7    $\langle a, \mu \rangle := (\mathcal{H}(\sigma.s \downarrow_{M_i}) \bmod |T_i|)$ -th element of  $T_i$  // schedule local transition
8    $s := \mathcal{U}_{pr}(\mu)$  // select next state according to  $\mu$ 
9 return  $s \in G$ 

```

# Fourth technique

## SMC + LSS of distributed schedulers

- ❖ Resolving non-determinism in SMC+LSS

$$\mathcal{H}(\sigma.s) \bmod n$$

- ❖ Resolving non-determinism in SMC+LSS+DS

$$\mathcal{H}(\sigma.(s \downarrow_{M_i})) \bmod n_i$$

bit vector limited  
to component  $i$

number of choices of  
component  $i$  at  $s$

**Input:** Network of VMDP  $M = \|_{SV}(M_1, \dots, M_n)$  with  $\llbracket M \rrbracket = \langle S, s_I, A, T \rangle$ ,  
goal set  $G \subseteq S$ ,  $\sigma \in \mathbb{Z}_{32}$ ,  $\mathcal{H}$  uniform deterministic, PRNG  $\mathcal{U}_{pr}$ .

```

1  $s := s_I$ 
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8    $s := \mathcal{U}_{pr}(\mu)$  // select next state according to  $\mu$ 
9 return  $s \in G$ 

```

### Sampling Distributed Schedulers for Resilient Space Communication

Pedro R. D'Argenio<sup>1,2,3</sup>, Juan A. Fraire<sup>1,2,3</sup>, and Arnd Hartmanns<sup>4</sup>

<sup>1</sup> CONICET, Córdoba, Argentina

<sup>2</sup> Saarland University, Saarbrücken, Germany

<sup>3</sup> Universidad Nacional de Córdoba, Córdoba, Argentina

<sup>4</sup> University of Twente, Enschede, The Netherlands  
a.hartmanns@utwente.nl

**Abstract.** We consider routing in delay-tolerant networks like satellite constellations with known but intermittent contacts, random message loss, and resource-constrained nodes. Using a Markov decision process model, we seek a forwarding strategy that maximises the probability of delivering a message given a bound on the network-wide number of standard probabilistic model checking would compute which are not implementable since

# Experiments (delivery probability)

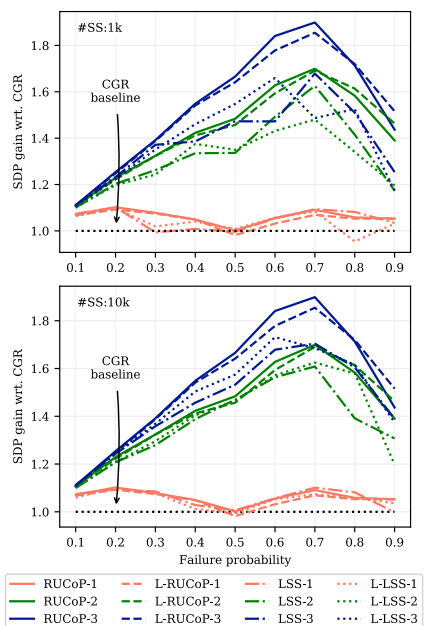


Figure 5: SDP gain over CGR in random networks.

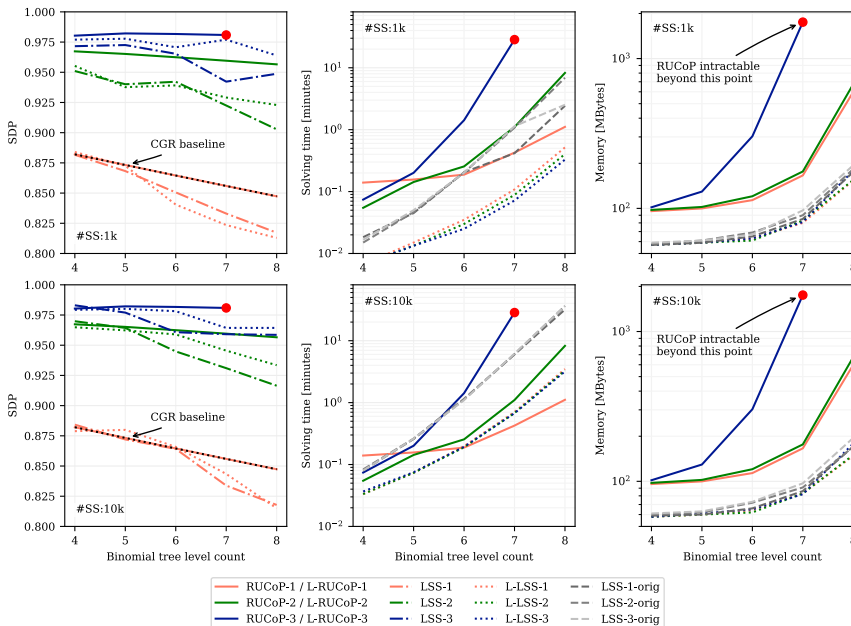


Figure 6: SDP, solving time, and memory for binomial networks with varying complexity (i.e., levels).

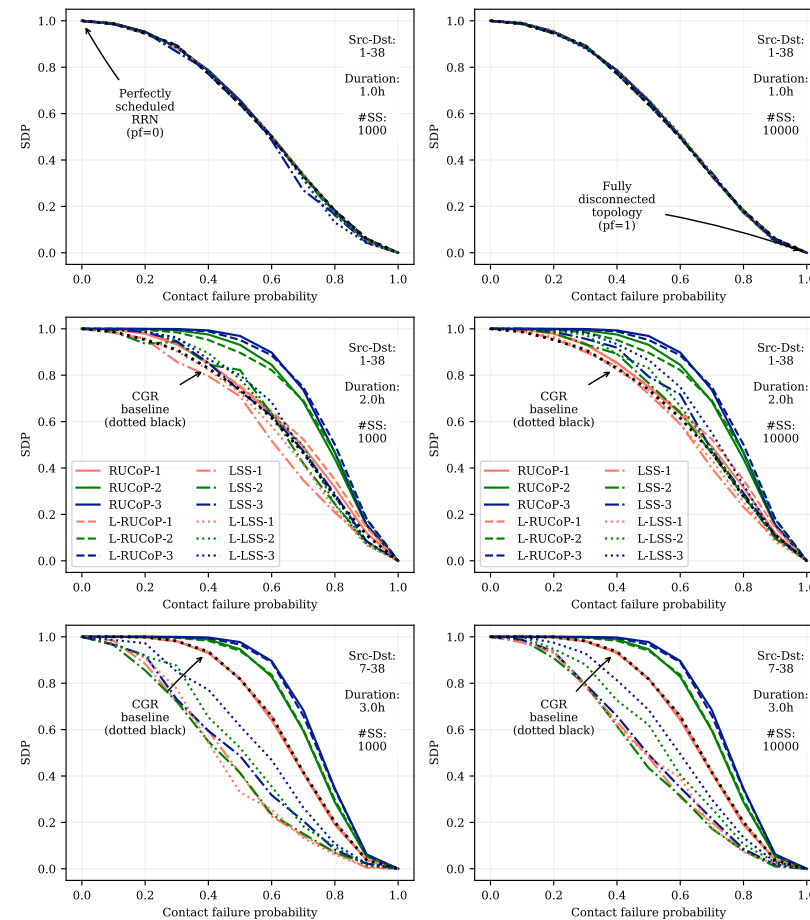
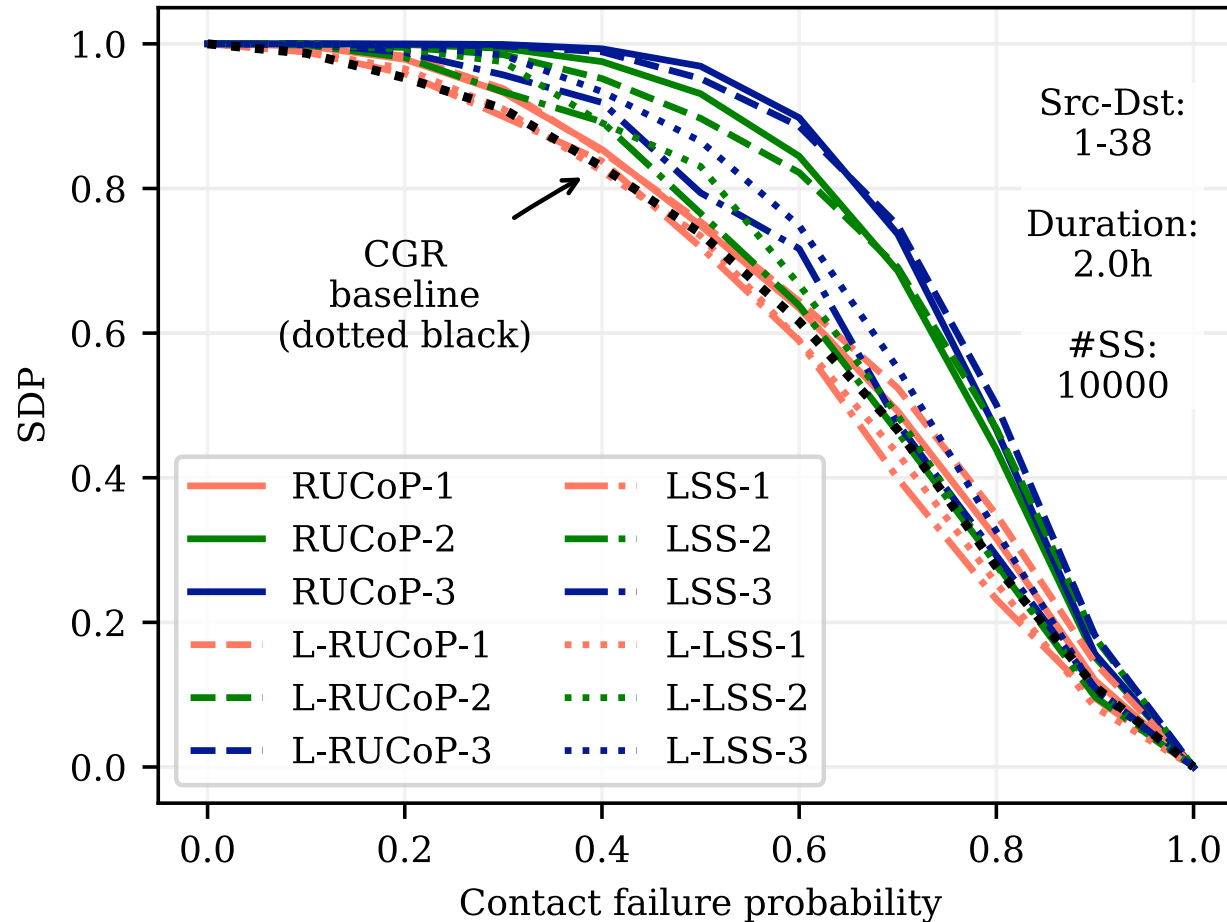


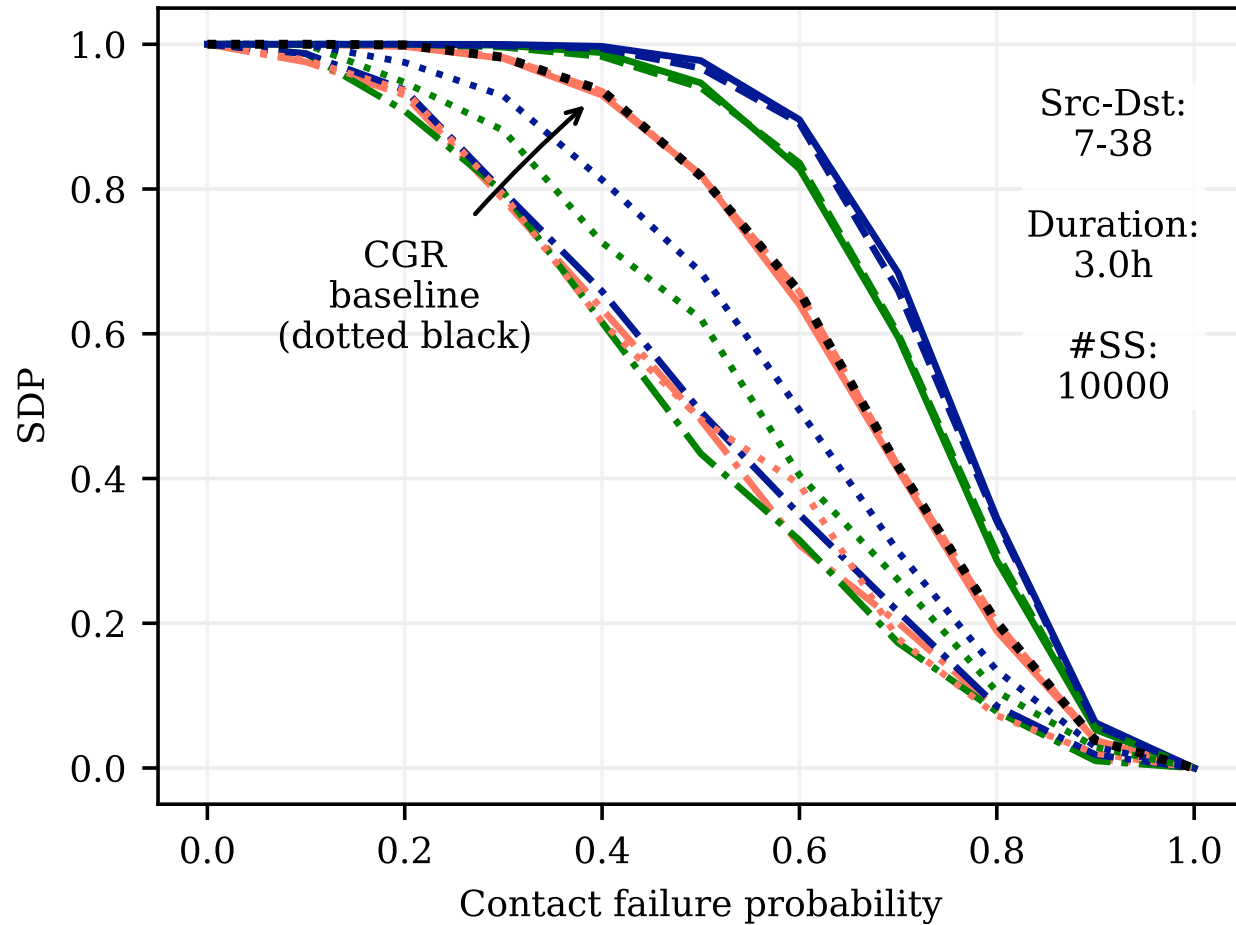
Figure 7: SDP for RRN for different source-target nodes, contact plan duration, and scheduler sampling.

# Experiments (delivery probability)





# Experiments (delivery probability)



# Experiments ( time & memory )

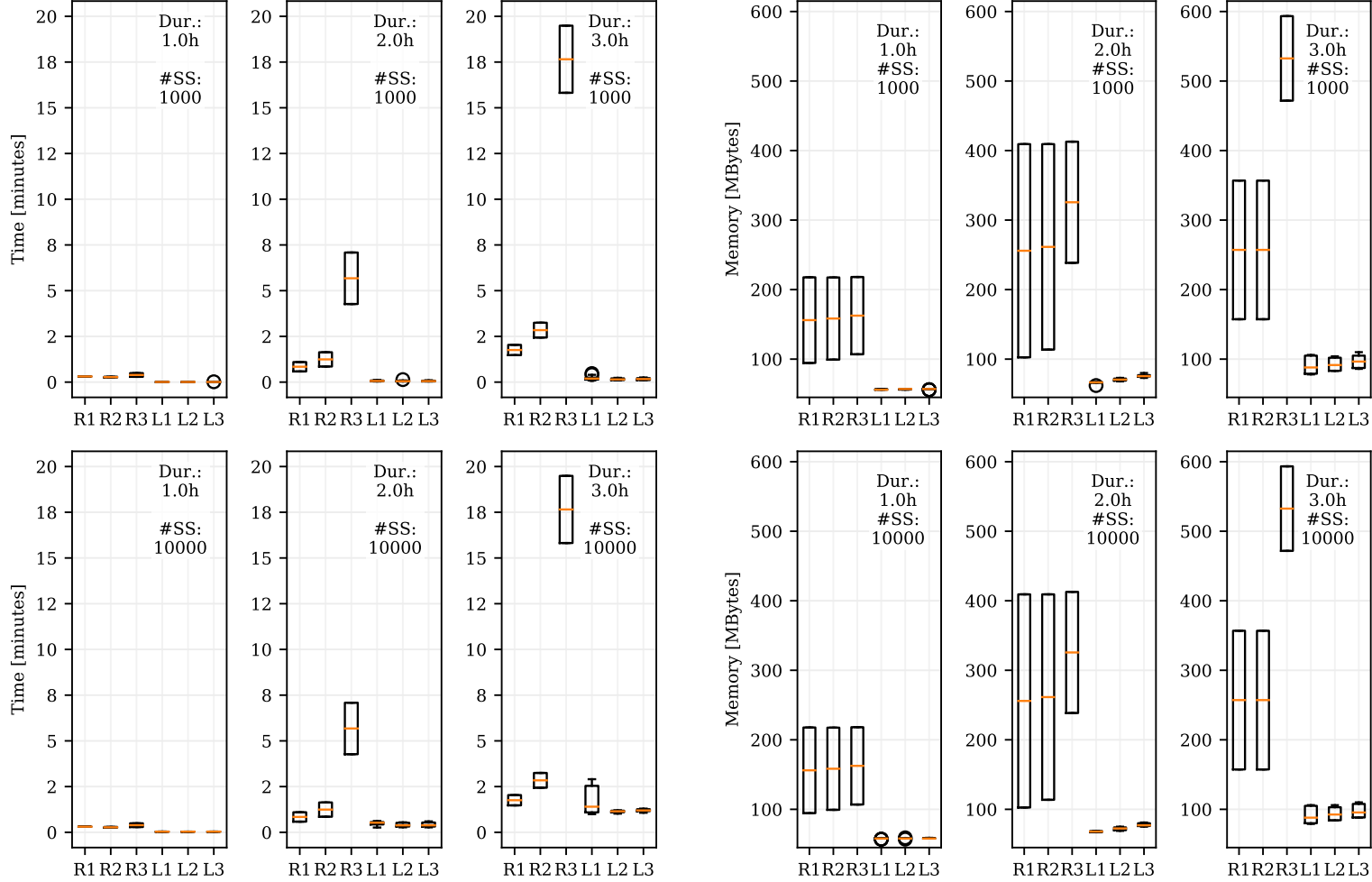


Figure 8: Solving time (left) and memory (right) for RRN for different source-target nodes, contact plan duration, and scheduler sampling (R = RUCoP, L = LSS).

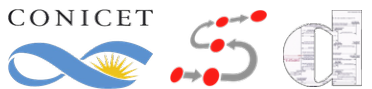
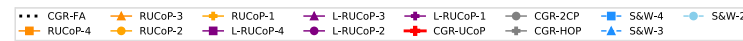
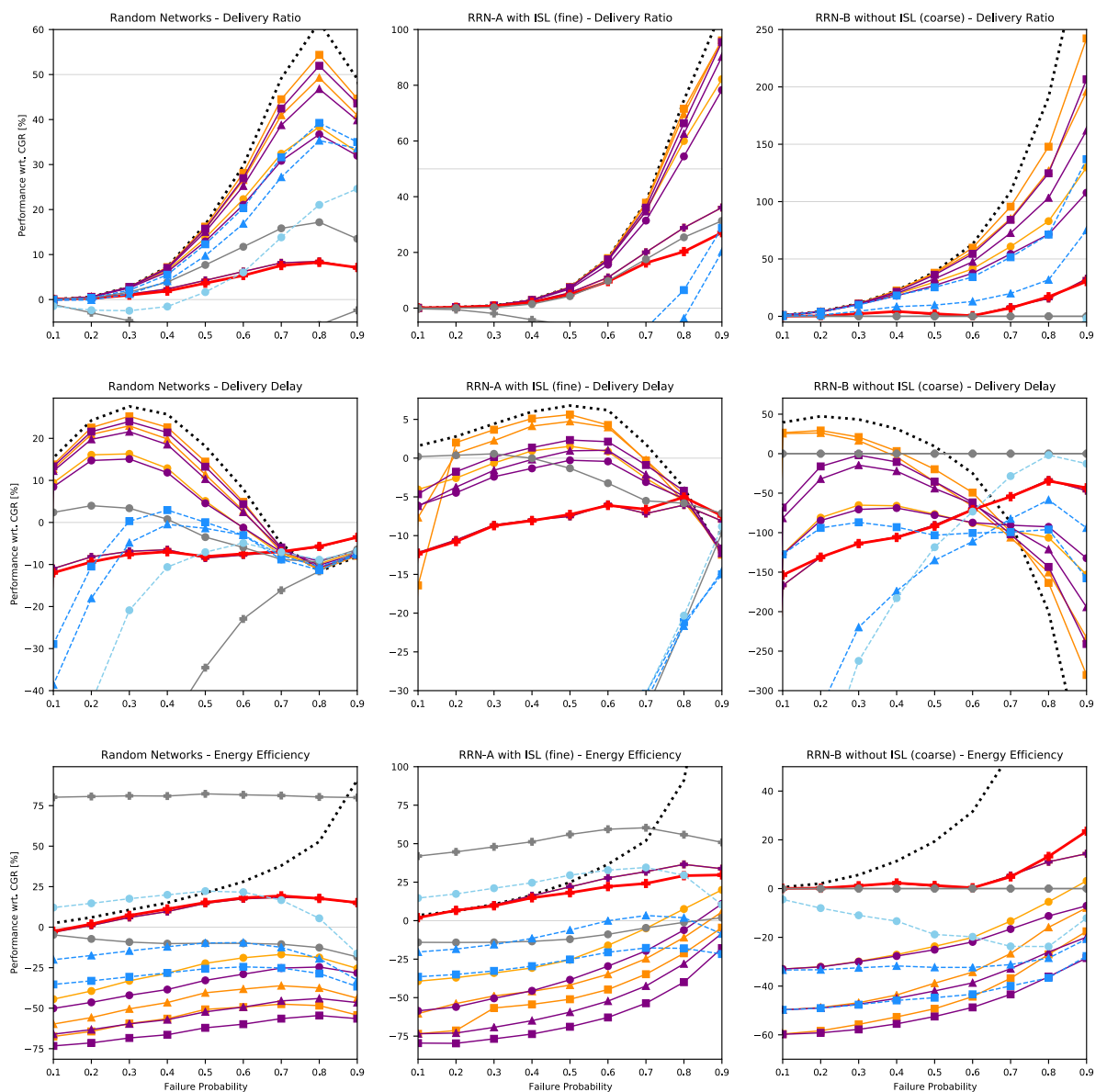
# Experiments (routing efficiency)

Probability

Latency

Energy

(Only RUCoP  
& L-RUCoP)



# Concluding remarks

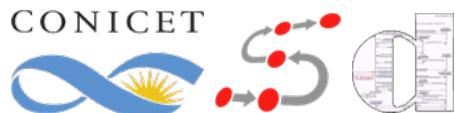
- ❖ Clear **increase of reliability** (particularly L-RUCoP & CGR-UCoP)
- ❖ **Comparison on latency is mixed**. It very much depends on probability of link failure
- ❖ Particularly, **(L-)RUCoP-1 & CGR-UCoP are more energy efficient** than CGR
- ❖ All algorithms are demanding:
  - ❖ Routing tables need to be calculated on ground and uploaded to the satellites
  - ❖ (CGR requires uploading the contact plan, routing decisions are made on flight)
  - ❖ CGR-UCoP requires uploading an annotated contact plan, routing decisions are made on flight. However, RUCoP is needed to annotate.

# Optimal Routing in Satellite DTN through Markov Decision Processes

Pedro R. D'Argenio

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